Vladimir Matveev

Suppose a closed manifold admits a metric of negative curvature. Then, any two metrics on the manifold have the same (unparameterized) geodesics if and only if they are proportional.